

## Schoenflies and Mulliken Notations

At the end of the 19<sup>th</sup> century Arthur Schoenflies developed the point group system shown in the table below to describe the external morphology of crystals. Crystallographers long ago abandoned this system in favour of the international (herman-maguin) approach but molecular scientists continue to use it. To find the equivalent point group in generator notation just compare the Schoenflies symbol with the generator symbol in the same position of the table.

Point groups in three dimensions - Schoenflies					
Partition	System	$G$	$\bar{G}$	$Gi$	
[1,1,1]	Triclinic	$C_1$		$C_i$	
	Monoclinic	$C_2$		$C_s$ $C_{2h}$	
	Orthogonal	$D_2$	$C_{2v}$	$D_{2h}$	
[2,1]	Trigonal	$C_3$		$S_6$	
		$D_3$	$C_{3v}$	$D_{3d}$	
	Tetragonal	$C_4$		$S_4$ $C_{4h}$	
		$D_4$	$C_{4v}$	$D_{2d}$ $D_{4h}$	
	Pentagonal	$C_5$		$S_{10}$	
		$D_5$	$C_{5v}$	$D_{5d}$	
	Hexagonal	$C_6$		$C_{3h}$ $C_{6h}$	
		$D_6$	$C_{6v}$	$D_{3h}$ $D_{6h}$	
	Heptagonal	$C_7$		$S_{14}$	
		$D_7$	$C_{7v}$	$D_{7d}$	
	Octagonal	$C_8$		$S_8$ $C_{8h}$	
		$D_8$	$C_{8v}$	$D_{4d}$ $D_{8h}$	
	.....				
	Infinity		$C_\infty$		$C_{\infty h}$
			$D_\infty$	$C_{\infty v}$	$D_{\infty h}$
[3]	Tetrahedral	$T$		$T_h$	
	Octahedral	$O$		$T_d$ $O_h$	
	Icosahedral	$I$		$I_h$	

## Irreducible representations in Mulliken notation

Mulliken notation for irreducible representations is closely associated with the Schoenflies notation for groups. For example,  $\bar{n}$  and  $\bar{n}2$  when  $n/2$  is an odd number have a peculiar standard Mulliken notation that includes primes (' and "). These groups are labeled  $C_{nh}$  and  $D_{nh}$  except for the special monoclinic case

Monoclinic $\bar{2}$ Schoneflies ( $C_s$ )	
$A$	$A'$
$B$	$A''$

Hexagonal $\bar{6}2$ Schoneflies ( $C_{3h}/D_{3h}$ )	
$A_1$	$A_1'$
$A_2$	$A_2'$
$B_1$	$A_1''$
$B_2$	$A_2''$
$E_1$	$E''$
$E_2$	$E'$

Dodecagonal $\bar{10}2$ Schoneflies ( $C_{5h}/D_{5h}$ )	
$A_1$	$A_1'$
$A_2$	$A_2'$
$B_1$	$A_1''$
$B_2$	$A_2''$
$E_1$	$E_1''$
$E_2$	$E_2'$
$E_3$	$E_2''$
$E_4$	$E_1'$

In groups  $\bar{n}$  and  $\bar{n}2$  when  $n/2$  is an even number all of the 2D irrep subscripts are reversed relative to the rotational group. Cyclic groups  $\bar{n}$  are Schoneflies  $S_n$  while  $\bar{n}2$  are  $D_{(n/2)d}$ .  $\bar{4}$  is no problem because there is only one 2D irrep.

Octagonal $\bar{8}2$ Schoneflies $S_8$	
$A_1$	$A_1$
$A_2$	$A_2$
$B_1$	$B_1$
$B_2$	$B_2$
$E_1$	$E_3$
$E_2$	$E_2$
$E_3$	$E_1$

Higher order groups follow the same complicated pattern

